Equivalence of neighborhoods of embedded compact complex manifolds and higher codimension foliations

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We consider an embedded n-dimensional compact complex manifold in $n+d$ dimensional complex manifolds. We are interested in the holomorphic classification of neighborhoods as part of Grauert's formal principle program. We will give conditions ensuring that a neighborhood of C_n in M_{n+d} is biholomorphic to a neighborhood of the zero section of its normal bundle. This extends Arnold's result about neighborhoods of a complex torus in a surface. We also prove the existence of a holomorphic foliation in M_{n+d} having C_n as a compact leaf, extending Ueda's theory to the high codimension case. Both problems appear as a kind linearization problem involving *small divisors condition* arising from solutions to their cohomological equations.